

Kaleidoscope of Heavy Electrons: Superconductivity, Magnetism, Quantum Critical Points

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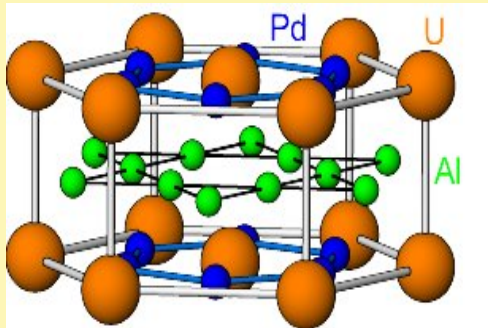
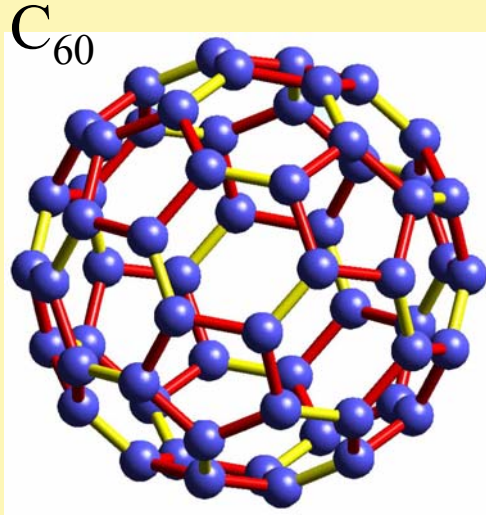
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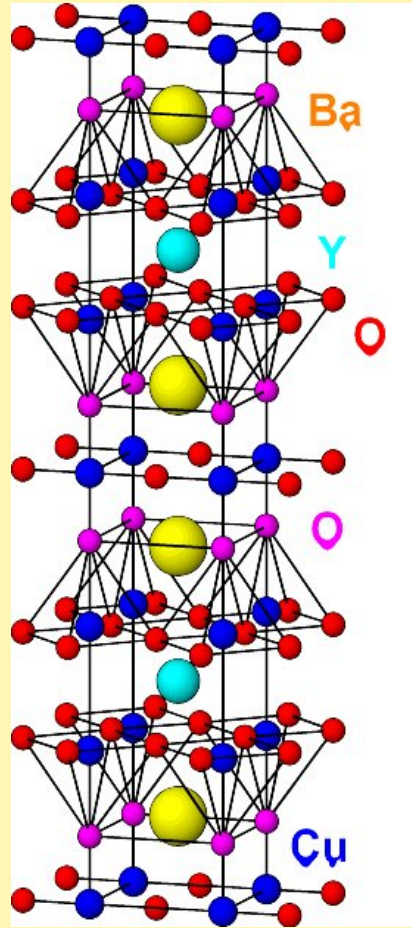
C. Pépin, CEA Saclay

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Crystal structures and phenomena



UPd_2Al_3



$YBa_2Cu_3O_7$

ferroelectricity

charge density wave

quantum Hall effect

1985, 98

conductivity in polymers

2000 (C)

superfluidity

1996, 2003

superconductivity (SC)

1913, 72, 73,
2003

high- T_c SC in cuprates

1987

colossal magnetoresistance

heavy fermions

quantum phase transitions

Outline

- Heavy-fermion (HF) metals
- Superconductivity
- Quantum criticality
- Outlook

Superconductivity in CeCu_2Si_2

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Superconductivity in the Presence of Strong Pauli Paramagnetism: CeCu_2Si_2

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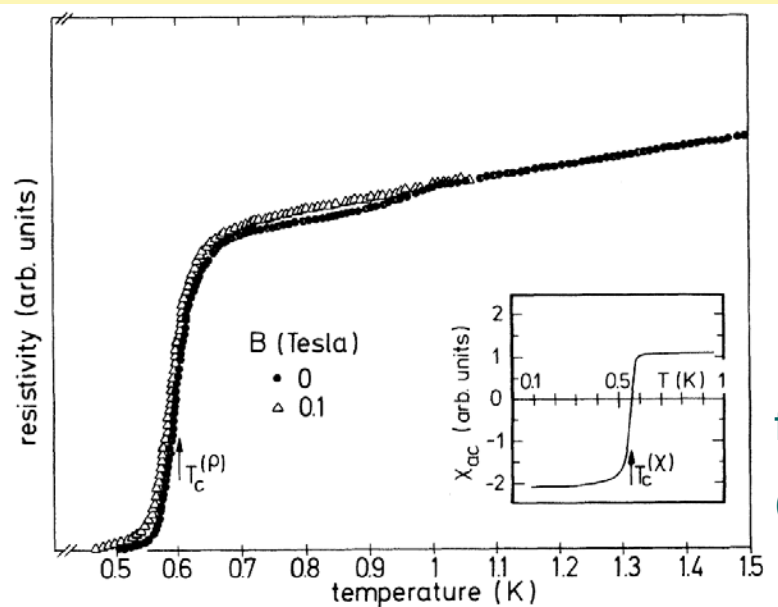
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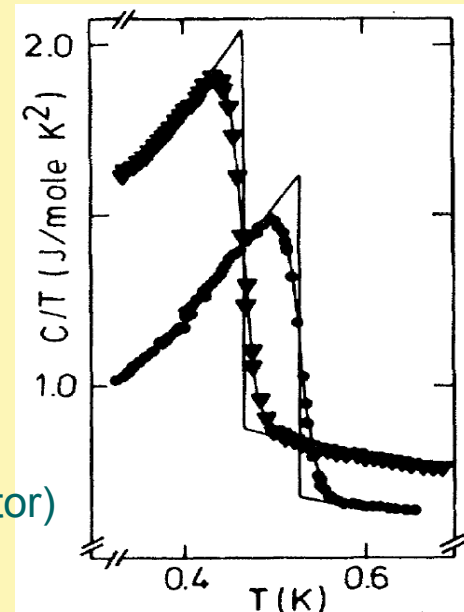
Eduard-Zintl-Institut, Technische Hochschule Darmstadt, D-6100 Darmstadt, West Germany

(Received 10 August 1979; revised manuscript received 7 November 1979)

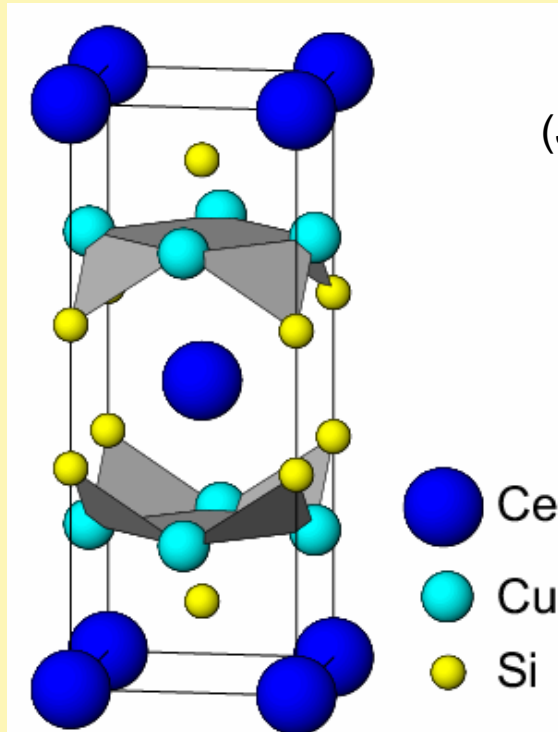


100 at% Ce^{3+} ions necessary
for superconductivity

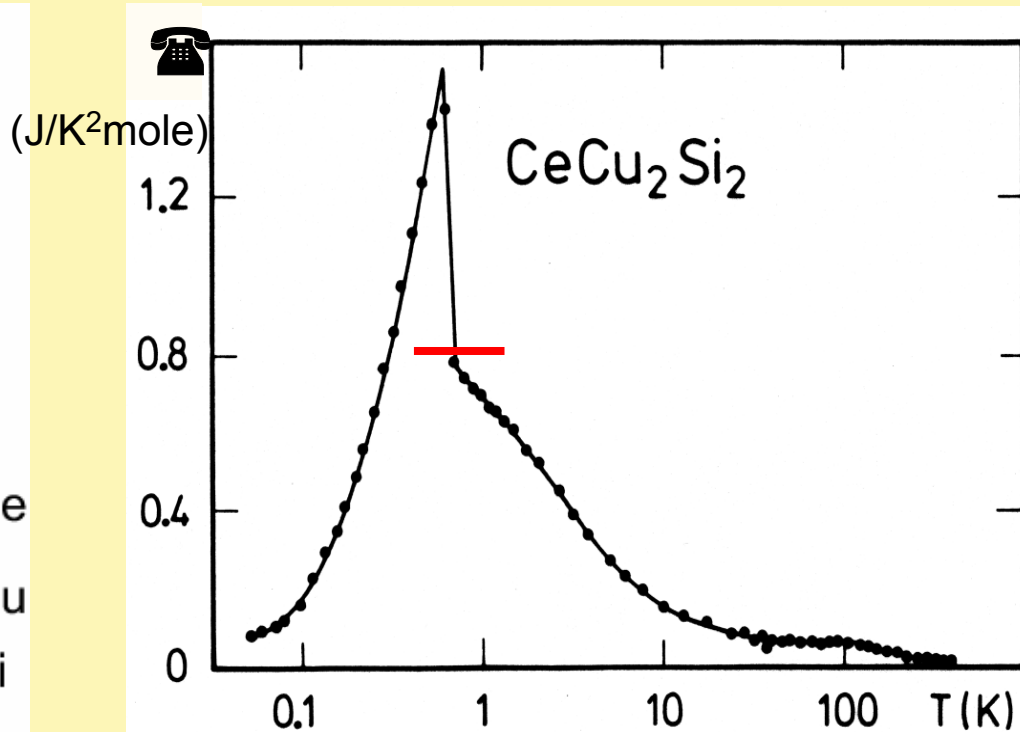
(LaCu_2Si_2 is not a superconductor)



Superconductivity of Heavy Fermions



- **Normal state**
($B_{c2} \approx 3$ Tesla)
- ☎ $\rightarrow 1 \text{ J/K}^2\text{mole}$ (Cu: $0.7 \cdot 10^{-3} \text{ J/K}^2\text{mole}$)
- Heavy Electrons**
("Heavy Fermions")



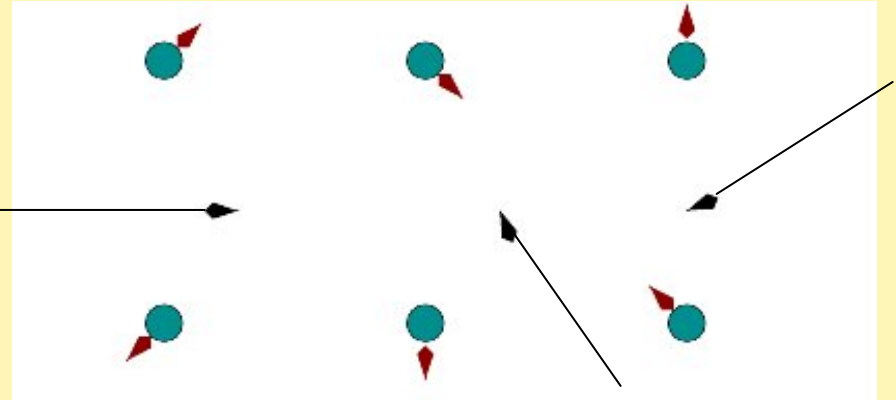
☎ $\sim m^*$
 $T_K \approx 15 \text{ K}$

- **Superconducting phase transition**
($B = 0$)
- $\Delta C/T_c \approx \text{☎}(T_c)$
- Cooper pairs formed by "Heavy Fermions"**
- Anisotropic order parameter**

Heavy-Fermion metals

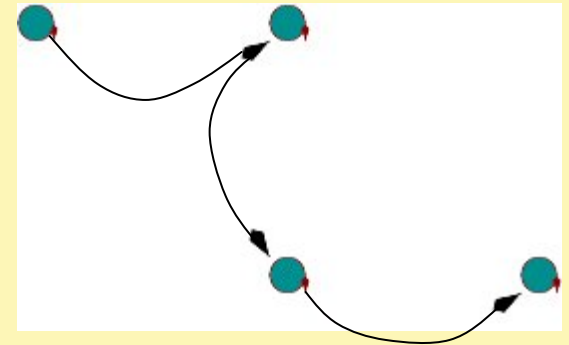
$$T \gg T_K \text{ (10 ... 100 K)}$$

$$v_F \approx 10^6 \frac{m}{s}$$



$T \ll T_K$: Heavy electrons ("composite fermions")

$$v_F^* \approx 10^3 \frac{m}{s}$$



→ $m^* \approx 1000 m_{el}$: "strongly correlated electron system"

Groundstate properties

- Heavy Landau Fermi liquid (LFL) : CeCu_6
- Non-Fermi liquid (NFL) : YbRh_2Si_2
- Magnetic order : NpBe_{13}
- Superconductivity : UPd_2Al_3

Heavy-Fermion Superconductors

Ce-based

T_c (K)

CeCu ₂ Si ₂	0.7	('79 DA/K)
[p = 2.9 GPa:	2.3	('84 GE/GR)]
CeNi ₂ Ge ₂	0.2	('97 DA, '98 CA/GR)
CeIn ₅	0.4	('00 LANL)
CeCoIn ₅	2.3	('00 LANL)
Ce ₂ CoIn ₈	0.4	('02 NA)
CePt ₃ Si	0.7	('03 VI)

p > 0

CeCu ₂ Ge ₂	0.6	('92 GE)
CeRh ₂ Si ₂	0.4	('95 LANL)
CePd ₂ Si ₂	0.4	('94 CA)
CeIn ₃	0.2	('98 CA)
CeRhIn ₅	2.1	('00 LANL)
Ce ₂ RhIn ₈	1.1	('03 LANL)

U-based

T_c (K)

UBe ₁₃	0.9	('83 Z/LANL)
UPt ₃	0.5	('84 LANL)
URu ₂ Si ₂	1.4	('84 K)
UNi ₂ Al ₃	1.2	('91 DA)
UPd ₂ Al ₃	2.0	('91 DA)

Pr-based

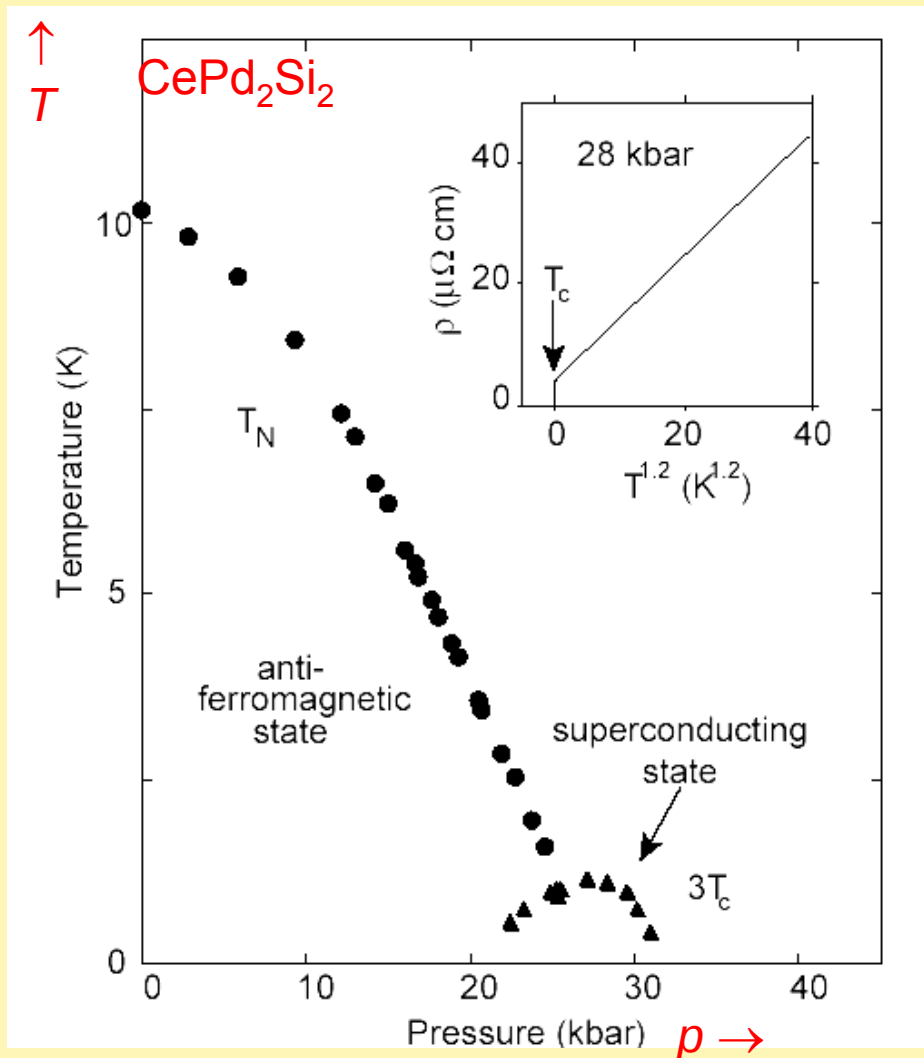
PrOs ₄ Sb ₁₂	1.85	('01 UCSD)
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Pu-based

PuCoGa ₅	18.5	('02 LANL)
PuRhGa ₅	8.7	('03 KA)

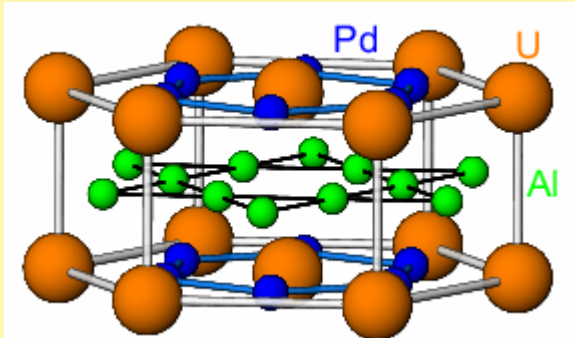
Non-Fermi-Liquid Superconductor: CePd_2Si_2

[N.D. Mathur et al., Nature **394**, 39 (1998)]



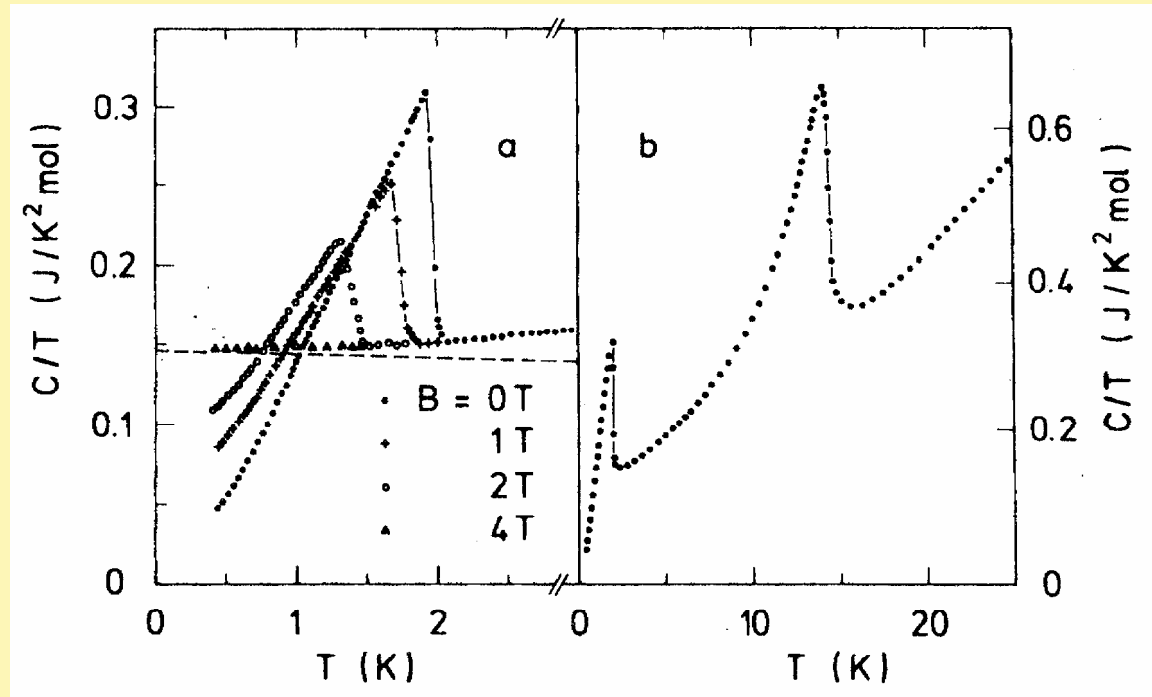
- AF QCP at $p_c = 28$ kbar
- $T_c = 0.4$ K at $p=p_c$
- NFL normal state
- SC mediated by strong spin-fluctuations ?

Magnetic Cooper pairing in UPd₂Al₃



C. Geibel et. al., 1991

$$\begin{aligned}
 T_{\text{magn}} &\approx 14 \text{ K} \\
 \mu_s &\approx 0.85 \mu_B \\
 \gamma &\approx 140 \text{ mJ/K}^2\text{mol} \\
 T_c &\approx 2 \text{ K} \\
 2\Delta_0/k_B T_c &\approx 6 \quad (\text{Kyougaku et al., 1993})
 \end{aligned}$$

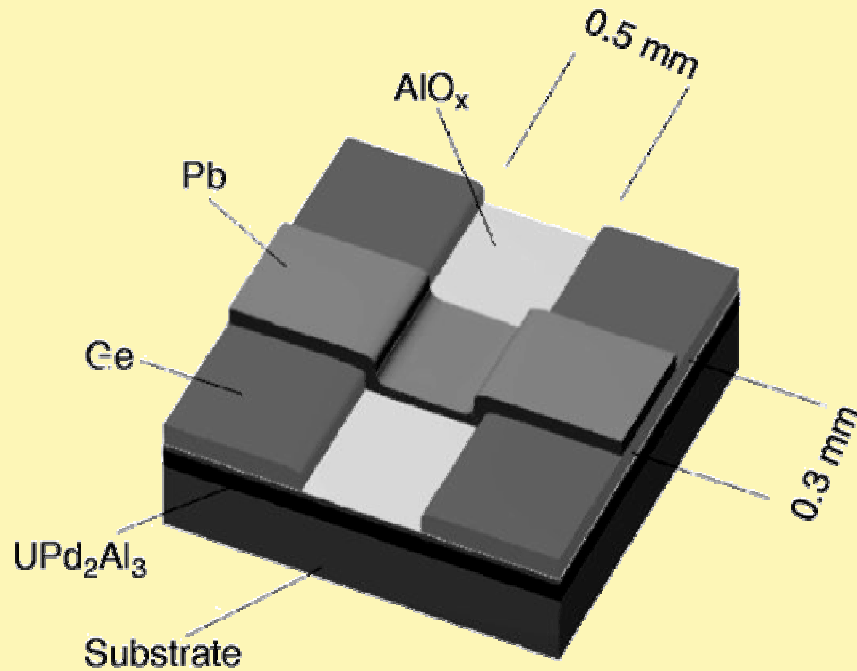


U³⁺ (5f³)

- **Two more localized ("core") electrons:** magnetism
 - **one less localized ("heavy" itinerant) electron:**
 - heavy LFL state ($T_c < T < T_N$)
 - heavy-fermion SC ($T < T_c$)
- coexisting with local AF

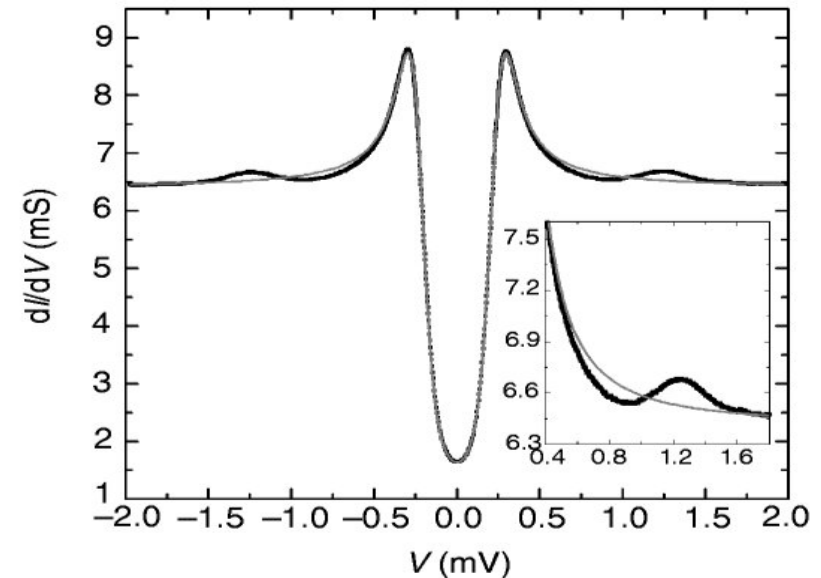
Quasiparticle tunneling

[M. Jourdan et. al., Nature **398**, 47 (1999)]



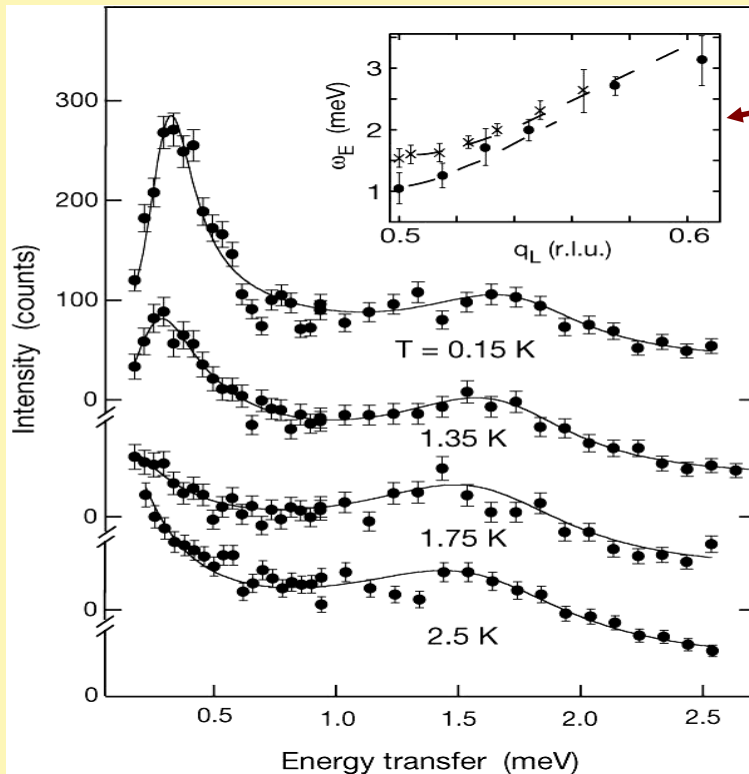
tunnel diode $\text{UPd}_2\text{Al}_3 - \text{AlO}_x - \text{Pb}$
(Pb normal conducting : $B = 0.3 \text{ T}$)

dI/dV
($T = 0.15 \text{ K}$)



Inelastic neutron scattering

[N.K. Sato et al., Nature **410**, 340 (2001)]

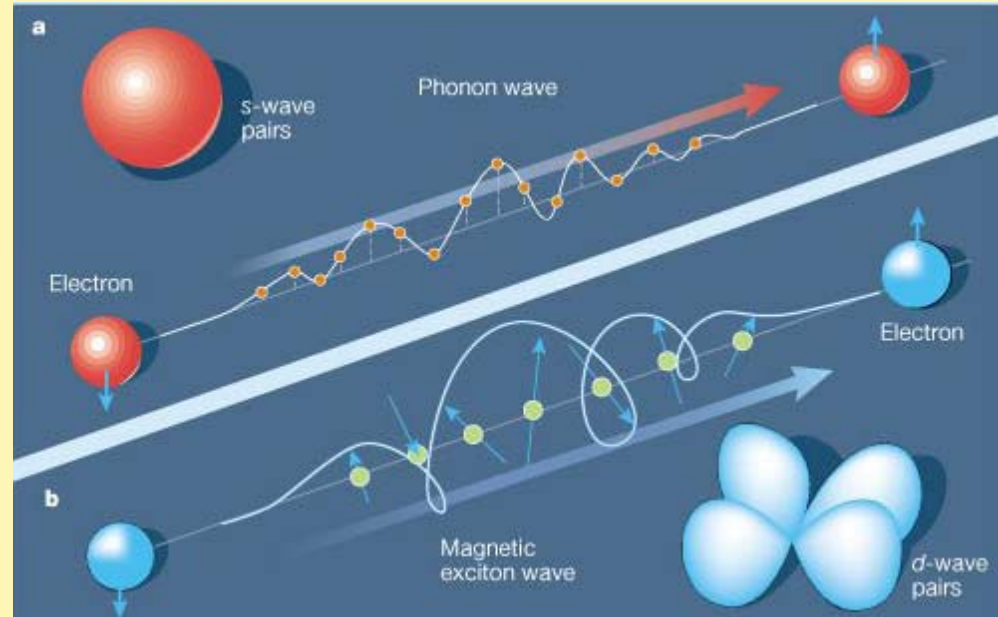


acoustic magnon
("magnetic exciton")

$$\vec{Q} = \vec{Q}_0 = (0, 0, 1/2)$$

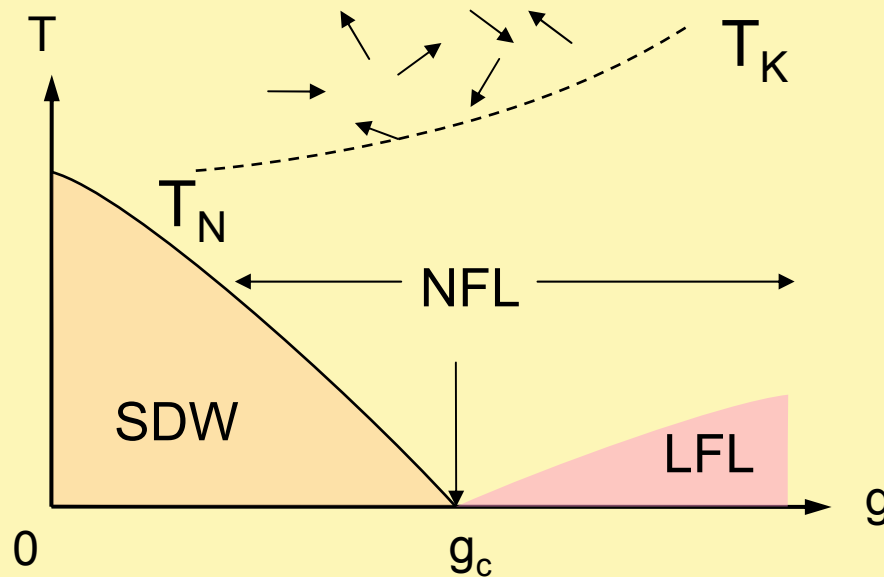
$$T_c = 1.8 \text{ K}$$

Cooper pairs formed by heavy electrons ("itinerant" 5f electrons)
superconducting glue provided by magnetic excitons in the system of
"localized" 5f electrons



Itinerant (SDW) scenario

*Moriya, Hertz,
Millis,
Continentino,
Lonzarich, ...*



$T < T_K$

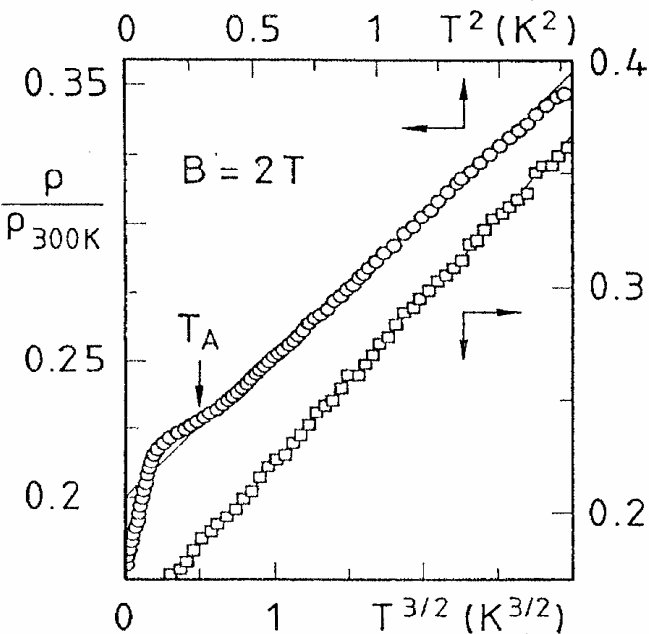
- local moments screened
- heavy QPs formed ("itinerant f-electrons")
- weak coupling: SDW phase
- QPs scattered off critical spin fluctuations

NFL

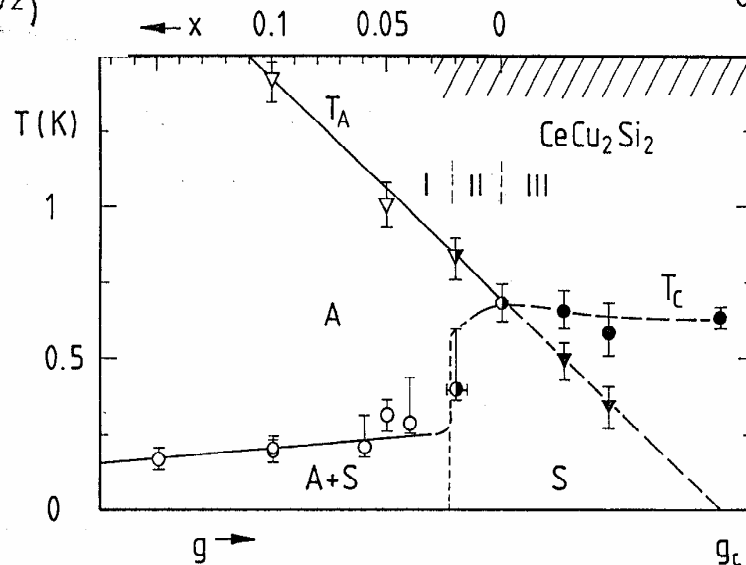
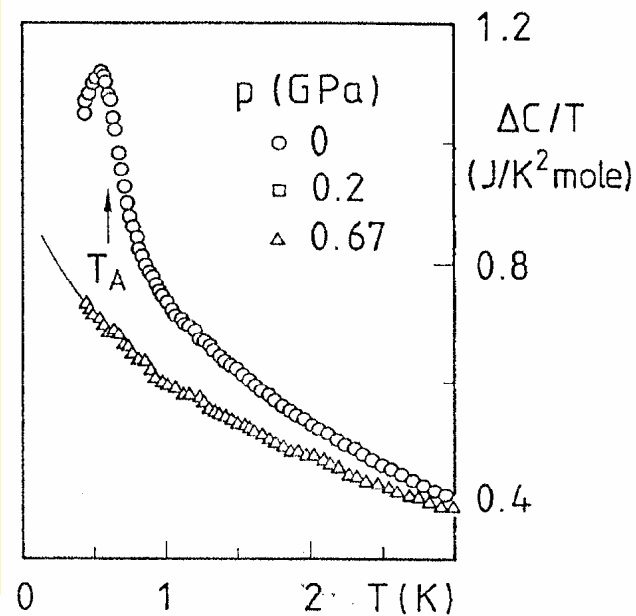
- in wide regions of phase diagram ($T, |g - g_c|$)
- thermal excitation of quantum critical modes
- coupling of statics and dynamics: $\tau_c \sim \xi^z$ (AF: $z = 2$); $d_{\text{eff}} = d + z$

CeCu₂Si₂: "A-S" transition at $p < 0.7$ GPa

[G. Sparn et al., Rev. High Press. Sci. Technol. 7, 431 (1998)]

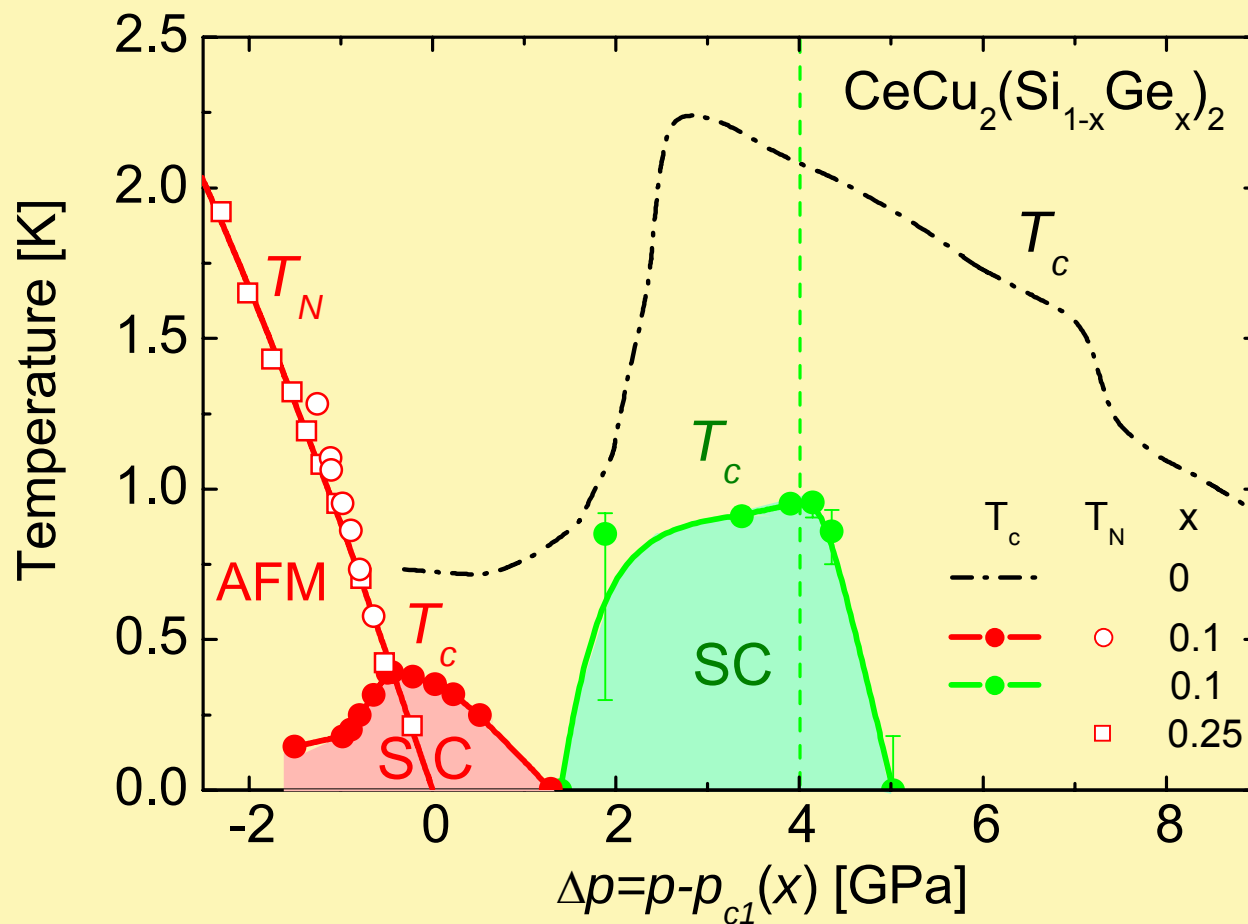


$p > p_c:$
 $\Delta\rho = \alpha T^{1.5}$
 $\gamma = \gamma_0 - \beta T^{0.5}$
 (3D-SDW scenario)



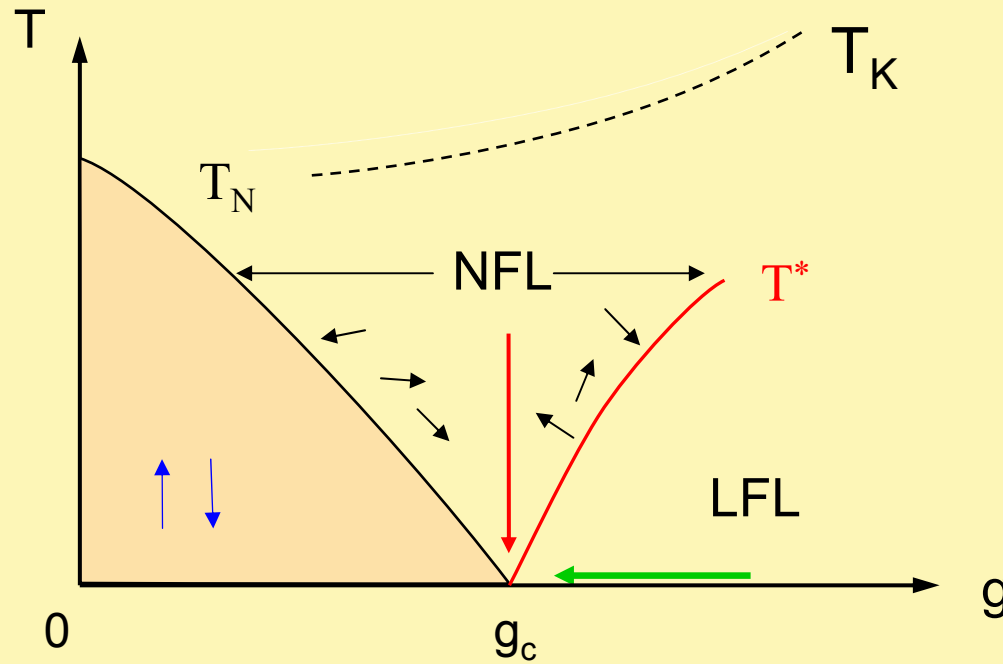
Observation of two distinct superconducting phases in CeCu_2Si_2

[H. Q. Yuan et al., Science **302**, 2104 (2003)]



Locally critical (local moment) scenario

*Schröder,
Coleman,
Si,
Pépin,
Ingersent,
Ramazashvili*

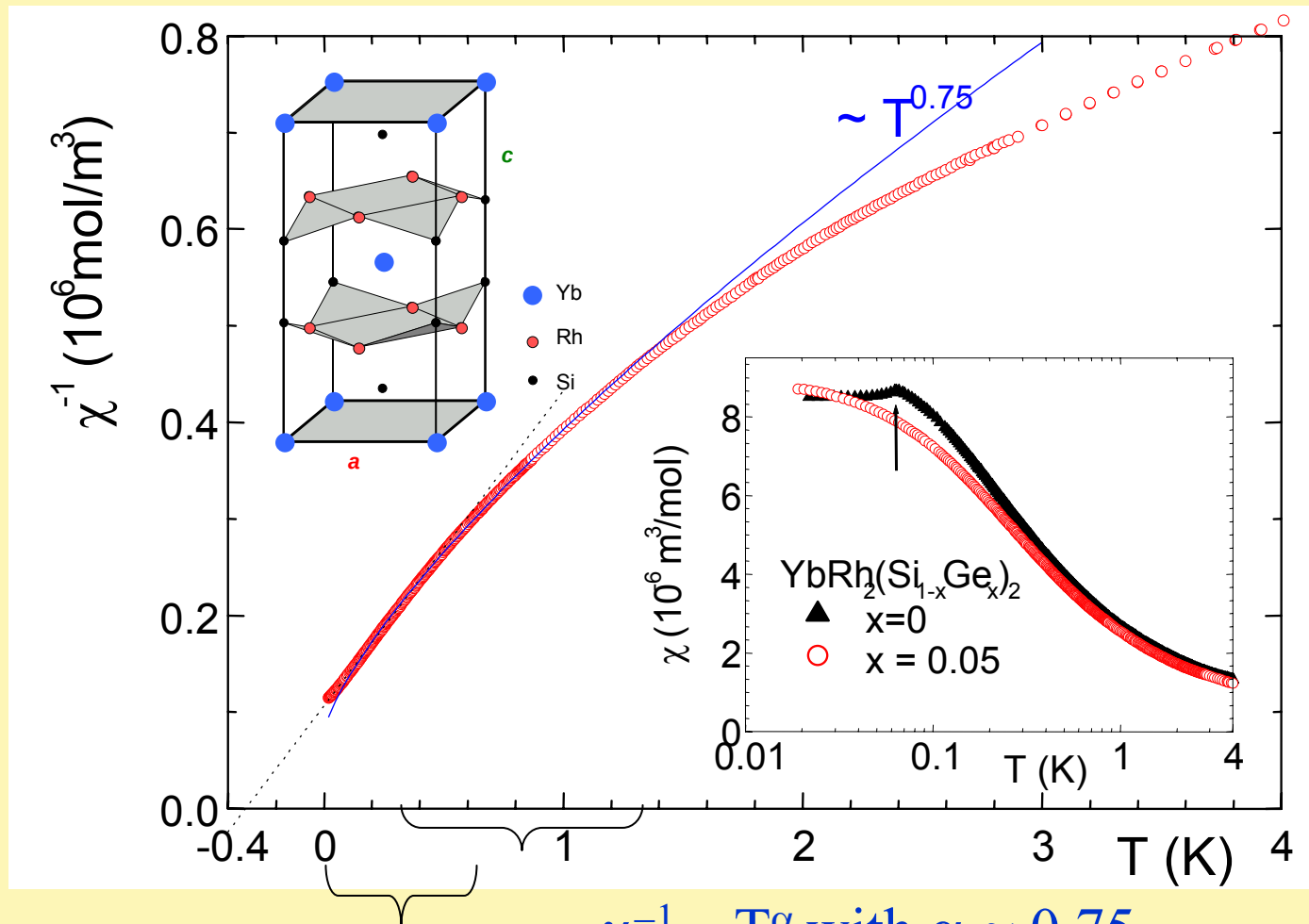


- Two QCPs coinciding: AFM - PM
LFL - NFL
- New quantum criticality dominating: **local** spin fluctuations
- At QCP: Kondo resonance not fully developed
- NFL: fluctuations between small and large Fermi surface

experimental techniques: T-dependence (at $g = g_c$)
g (p or B) -dependence (at $T = 0$)

YbRh₂(Si_{0.95}Ge_{0.05})₂

[P. Gegenwart et al., Acta Pol. Phys. B **34**, 323 (2003)]



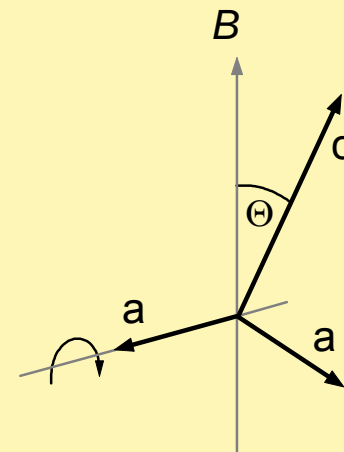
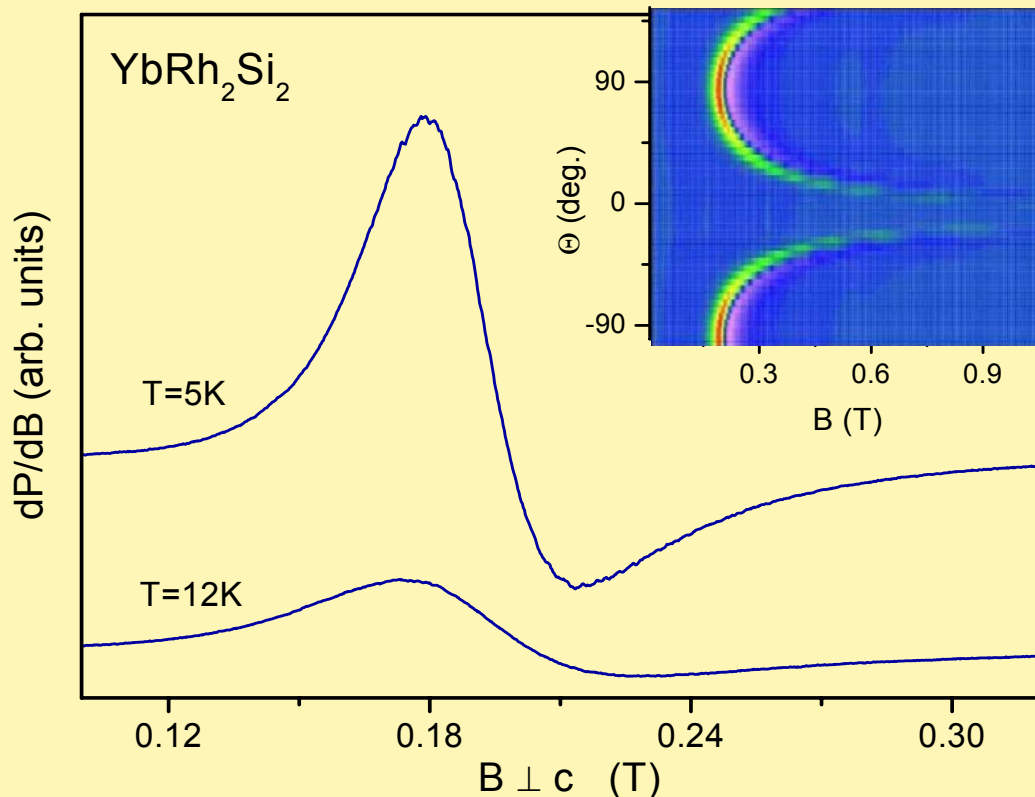
$$\chi = C/(T-\theta)$$

$$\theta = -0.3 \text{ K}$$

$$C \rightarrow \mu_{\text{para}} = 1.4 \mu_B/\text{Yb}^{3+}$$

Yb³⁺ ESR in YbRh₂Si₂

[J.Sichelschmidt et al., PRL **91**, 156401 (2003)]



$$g_{\perp} = 3.561 \pm 0.006$$

$$g_{\parallel} = 0.17 \pm 0.07$$

linewidth $\Delta B_{\text{exp}} = 0.02\text{ T} \ll \Delta B_K = k_B T_K / \mu_B = 37\text{ T} \quad (T_K = 25\text{ K})$

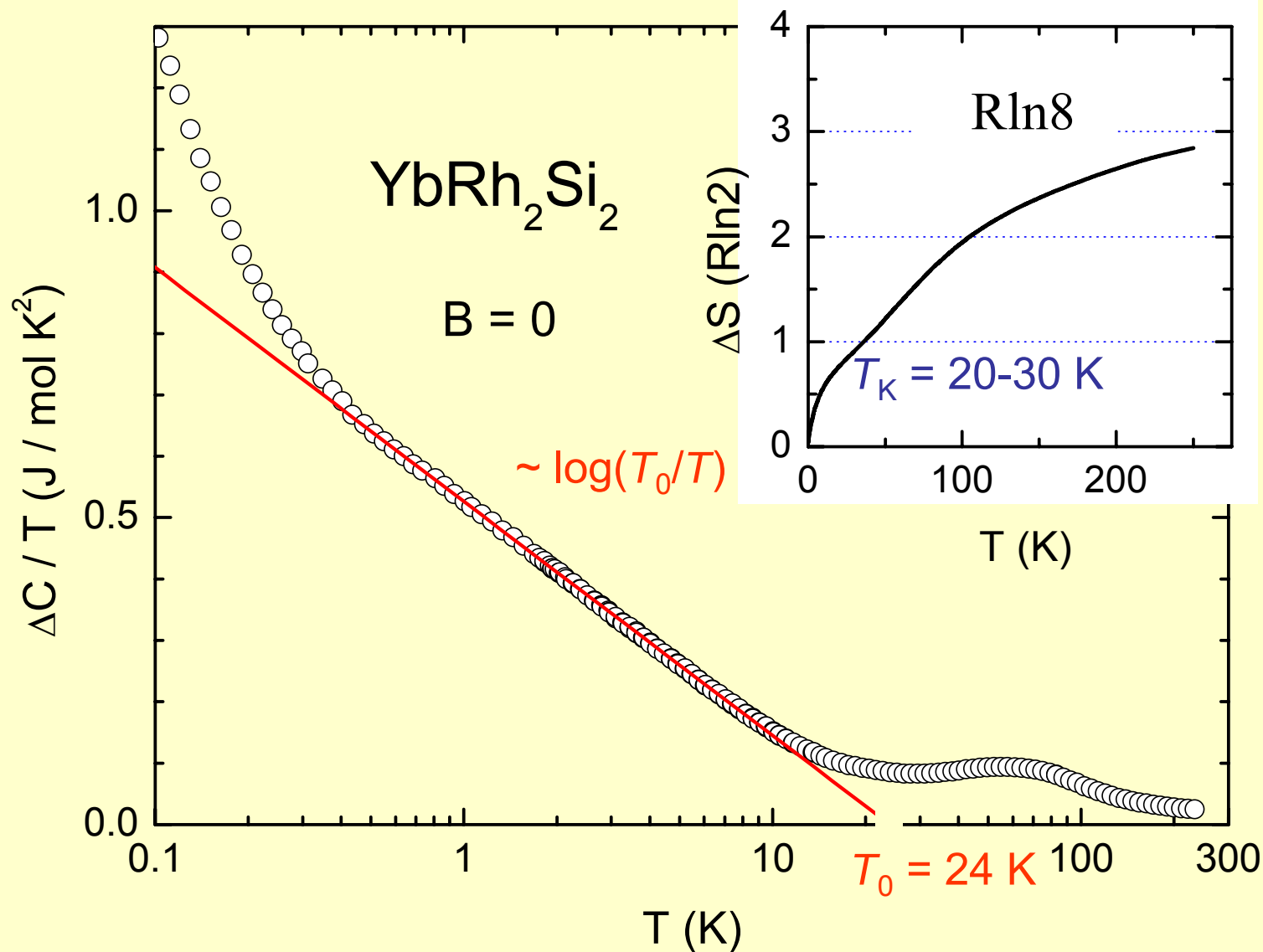
intensity $I \sim \chi(\omega = 0, \mathbf{q} = 0)$

anisotropy

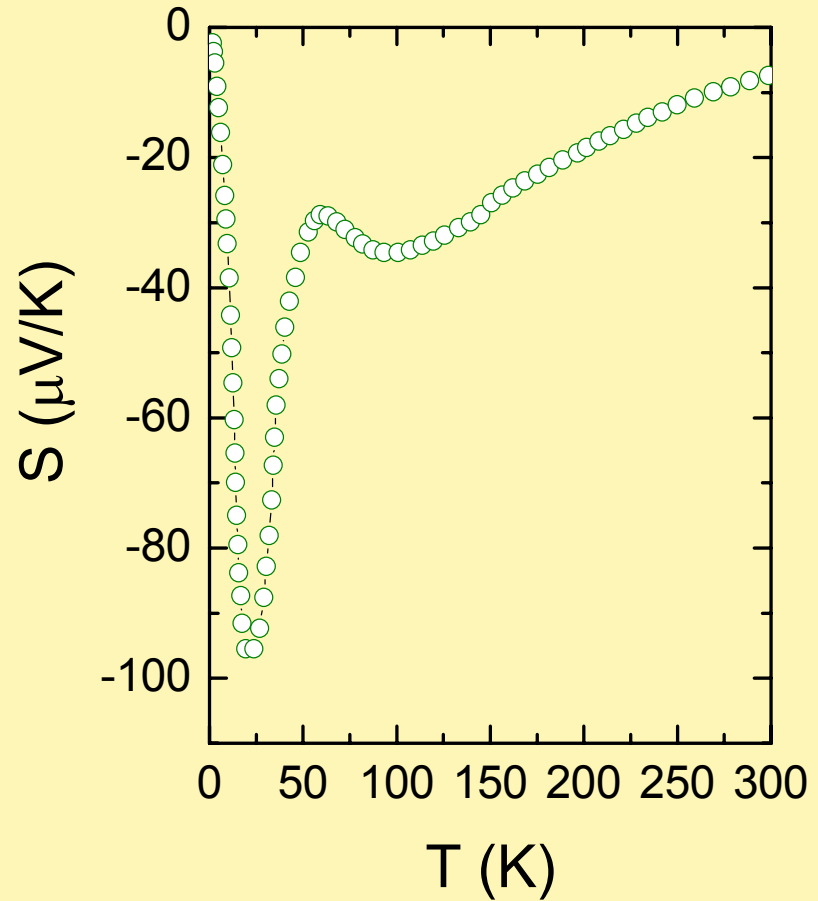
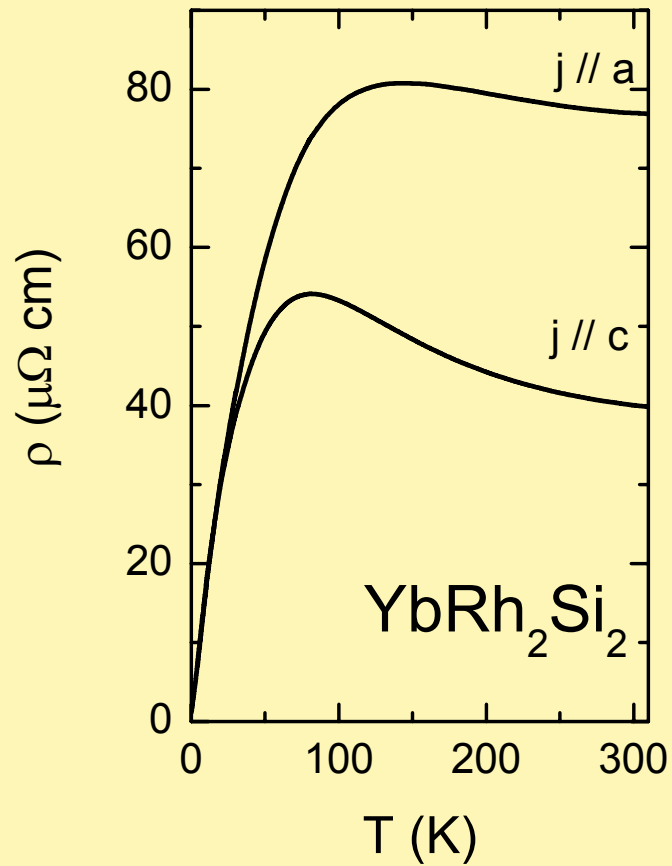


large local Yb³⁺ moments exist well below $T_K = 25\text{ K}$

Kondo temperature T_K from thermodynamics

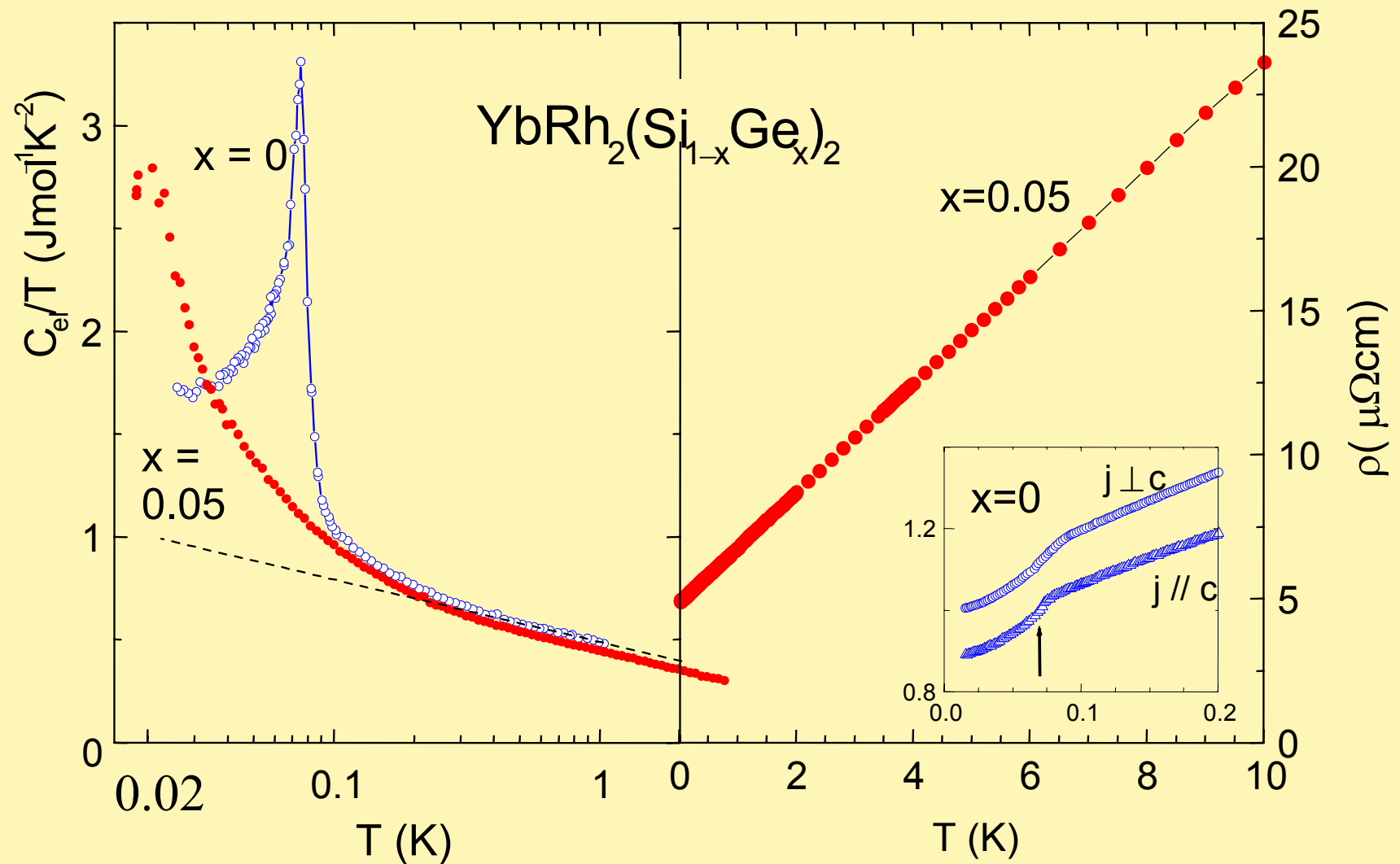


Kondo temperature T_K from transport

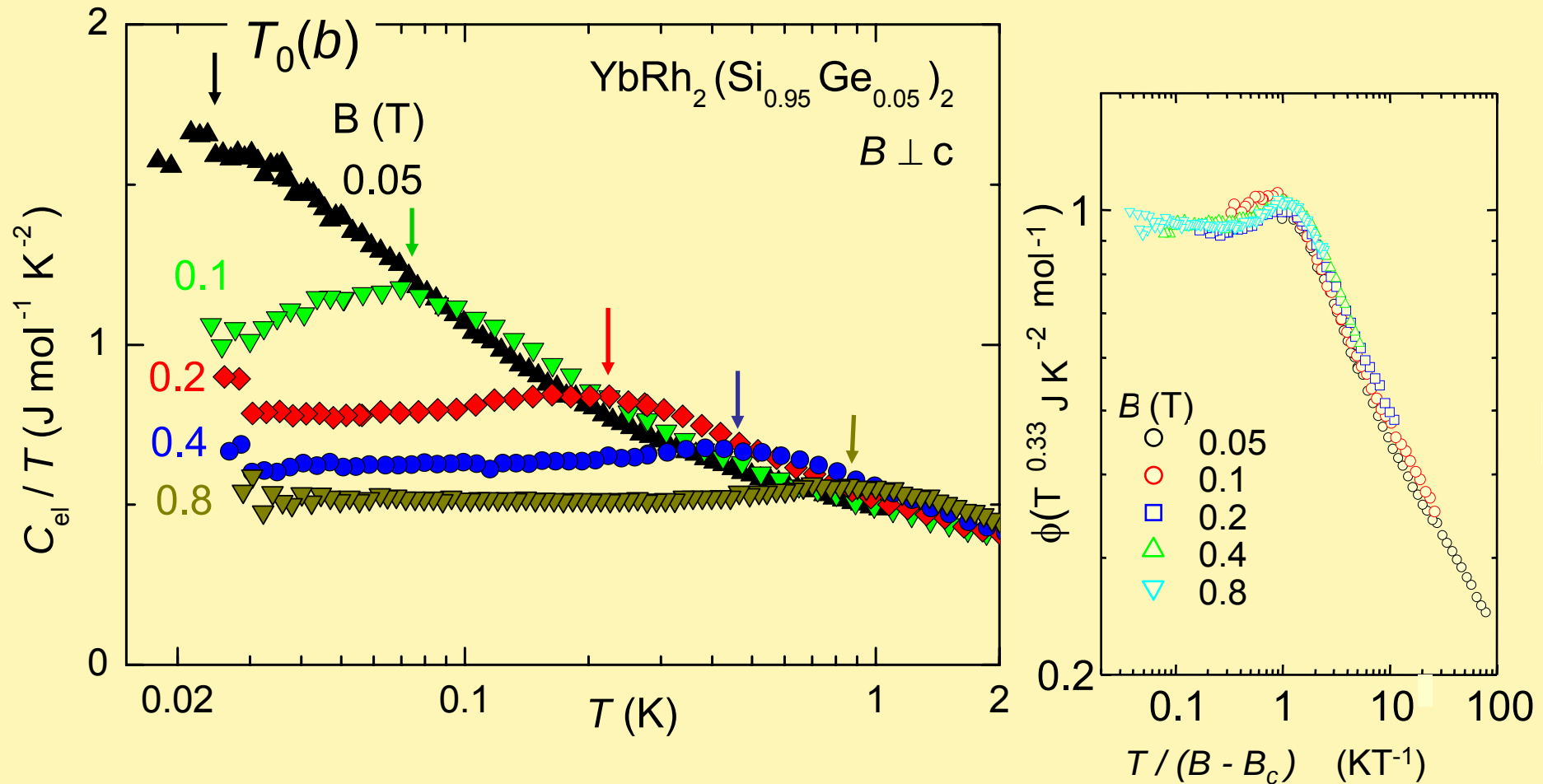


Disparity between C_{el}/T and ρ in YbRh_2Si_2

[J. Custers et. al., Nature **524**, 424 (2003)]



Scaling behavior in $C_{el}(T,b)/T$; $b = B - B_c$

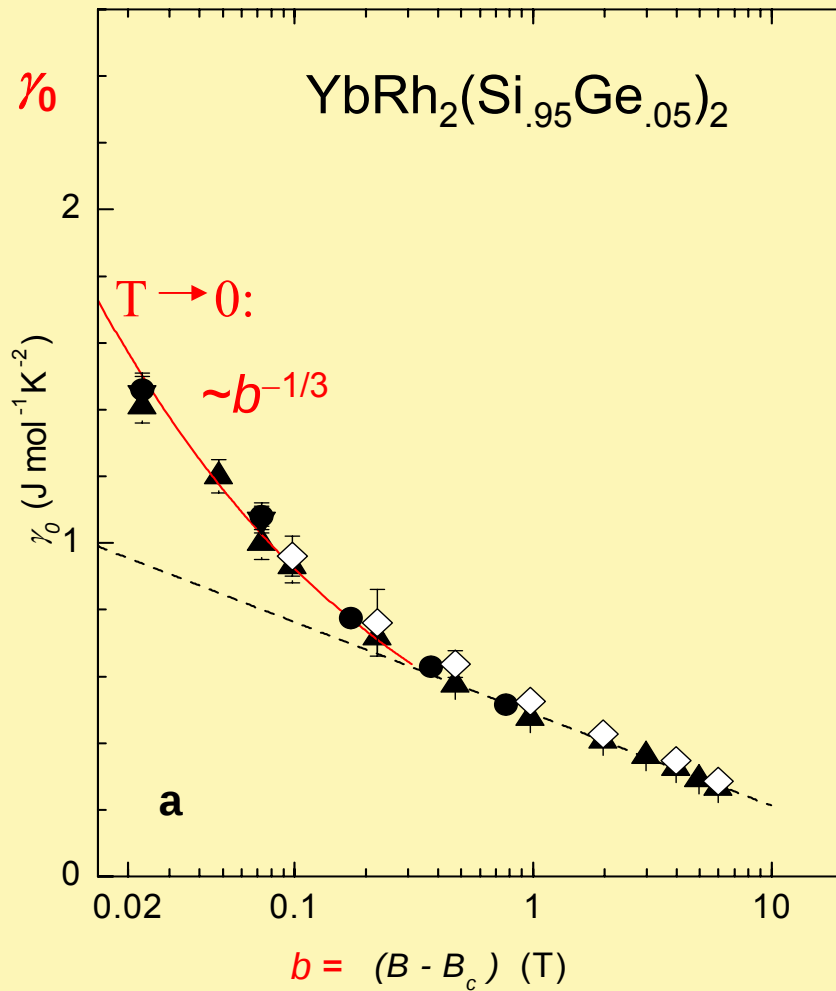


Characteristic energy scale $T_0(b) \sim b$ vanishes at QCP

$\Rightarrow T/T_0$ scaling for $\Phi(T,b)$ with $\Phi(T,b) = b^{1/3} \cdot C(T,b)/T$

$\Rightarrow S(T,b) = b^{2/3} S(T/T_0) \rightarrow 0$ at QCP $\Rightarrow$ no residual entropy at QCP

Field dependence of $\gamma_0(b)$, $b \perp c$ ($B_c = 0.027$ T)



Similar: $\frac{T^2}{\Delta \rho} = A^{-1} \sim$

T ($b \rightarrow 0$)
b ($T \rightarrow 0$)

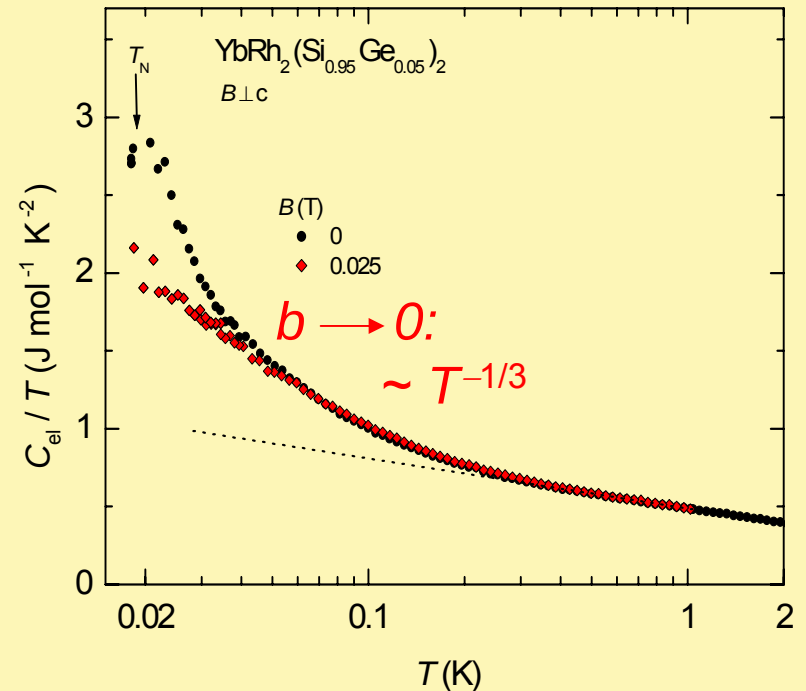
$\gamma \sim (-\log b)$ for $b \geq 0.3$ T

$b^{-1/3}$ ($b \rightarrow 0$)

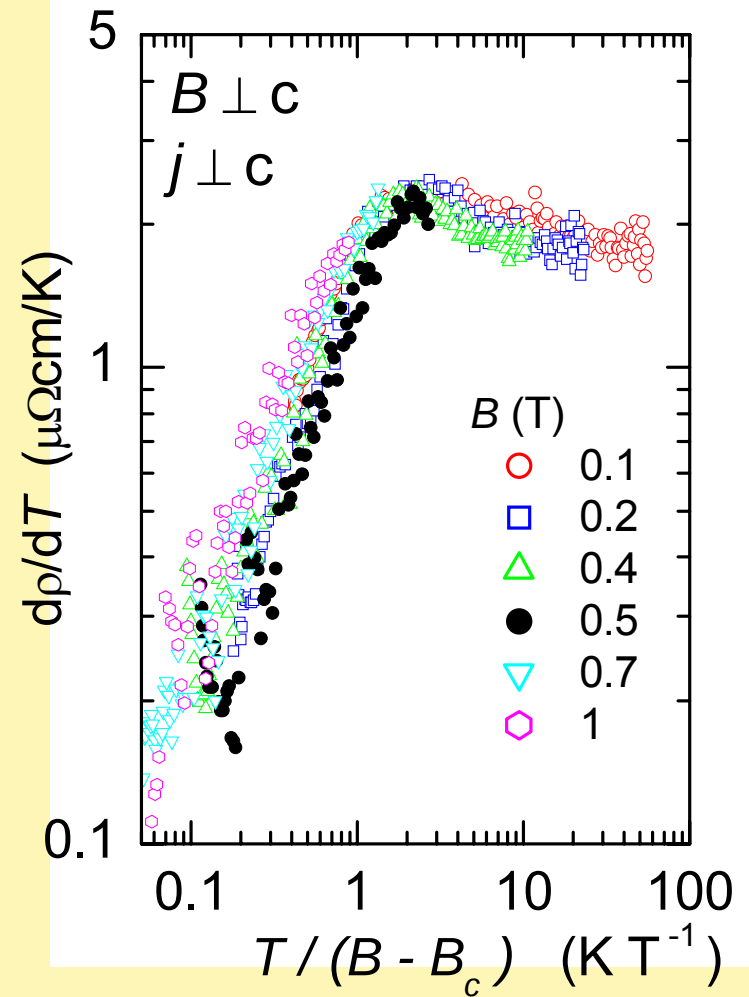
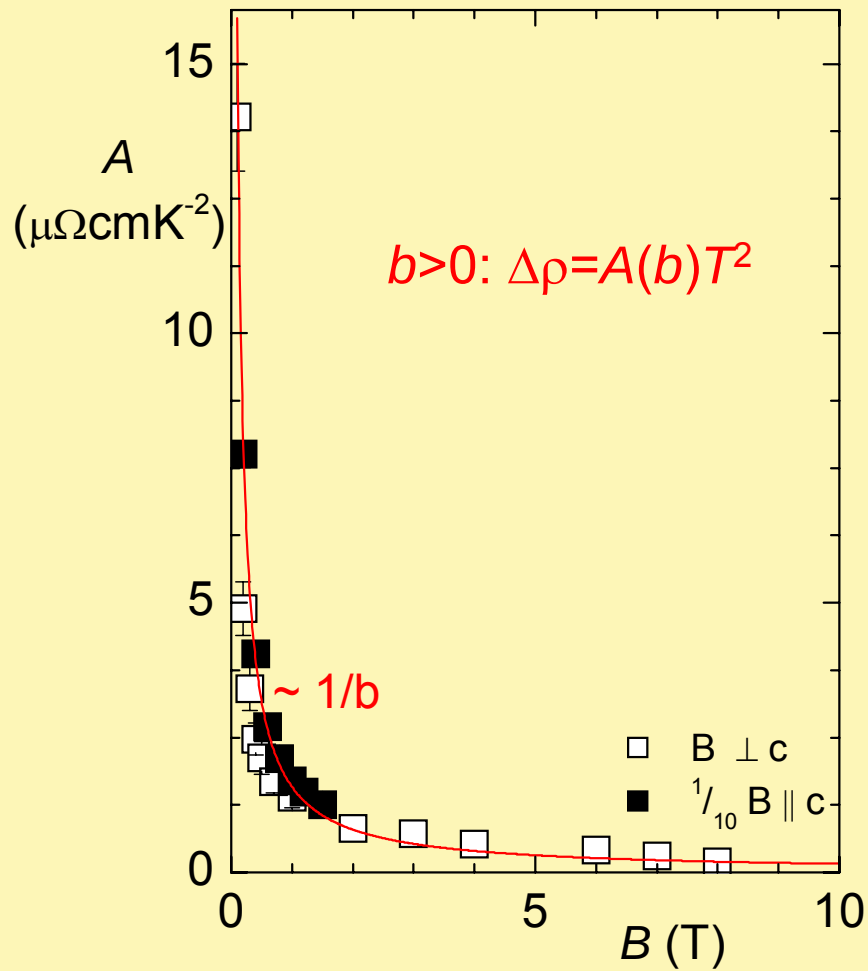
$\Rightarrow$ contradiction to 2D-SDW scenario

$\Rightarrow b$ -dependence at $T=0$ similar to

T -dependence at $b=0$



Scaling behavior in $\rho(T,b)$, $b = B - B_c$



Grüneisen ratio

[R. KÜchler et al., PRL **91**, 066405 (2003)]

Specific heat: $C/T \sim \partial S / \partial T$

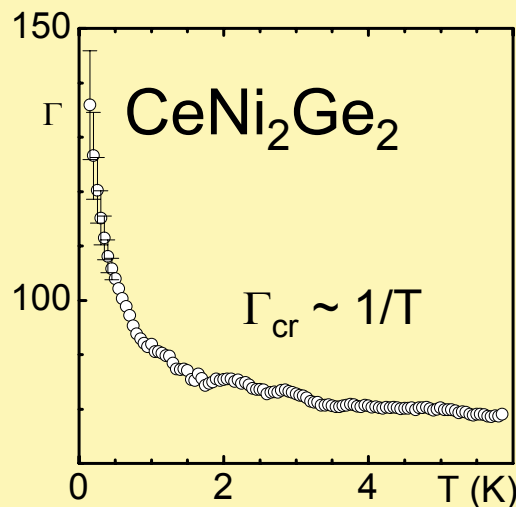
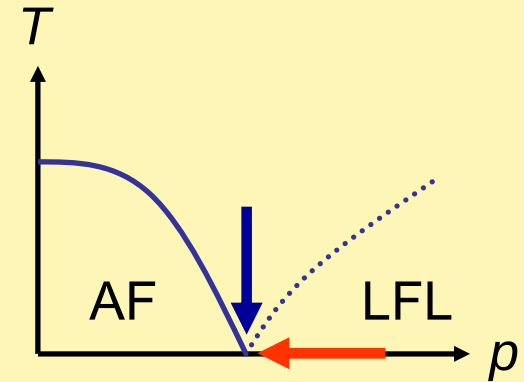
Thermal expansion: $\beta \sim (-\partial S / \partial p)$

($\beta = 1/V dV/dT$)

L. Zhu, M. Garst, A. Rosch, Q. Si, PRL **91**, 066404 (2003):

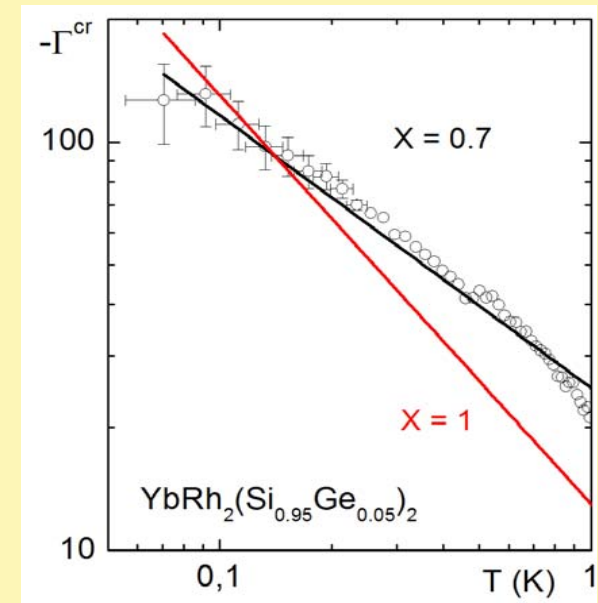
Grüneisen ratio $\Gamma_{cr} = \beta_{cr} / C_{cr}$ diverges at any QCP, $\Gamma_{cr} \sim T^{-x}$

Critical exponent $x \longrightarrow$ nature of QCP



$x = 1$:

3D-SDW scenario



Outlook

Importance of **local f-degrees of freedom**, e.g.,

UPd_2Al_3 - Cooper pairing via (propagating) **local 5f-excitation**

$\text{YbRh}_2(\underline{\text{Si}}, \text{Ge})_2$ - suggestive of **local QCP**

- ★ non-Kondo-screened fluctuating **Yb^{3+} moments**

- ★ **break-up** of heavy ("composite") quasiparticles

- ★ **fractional exponent** for Grüneisen ratio

- **no** superconductor

However:

CeCu_2Si_2 - compatible with (3D) SDW scenario, superconductors

CeNi_2Ge_2

⋮



Is **local QCP unfavorable** for superconductivity?



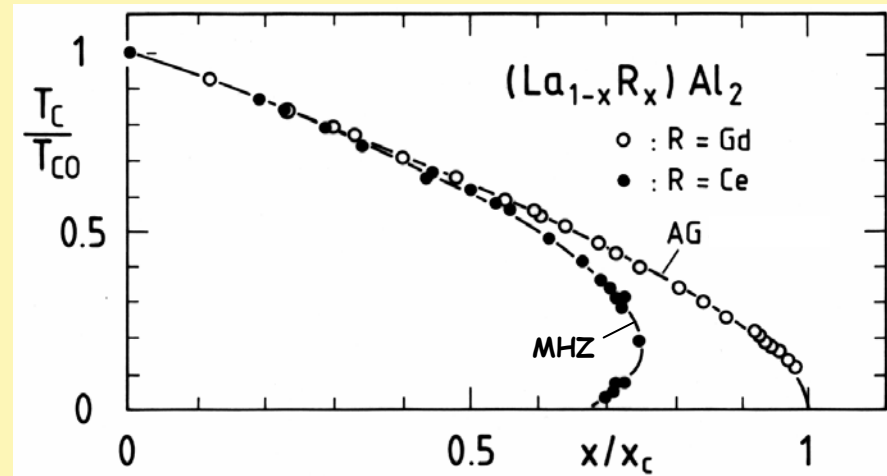
Superconductivity vs. magnetism

IA																VIII A																									
1 H 1.008																2 He 4.003																									
3 Li 6.941																10 Ne 20.18																									
4 Be 9.012																18 Ar 39.95																									
11 Na 22.99		12 Mg 24.31														19 K 39.10		20 Ca 40.08		37 Rb 85.47		38 Sr 87.62		55 Cs 132.9		56 Ba 137.3		87 Fr (223)													
13 Al 26.98		14 Si 28.09		15 P 30.97		16 S 32.07		17 Cl 35.45		21 Sc 44.96		22 Ti 47.87		23 V 50.94		24 Cr 52.00		25 Mn 54.94		26 Fe 55.85		27 Co 58.93		28 Ni 58.69		29 Cu 63.55		30 Zn 65.39		31 Ga 69.72		32 Ge 72.61		33 As 74.92		34 Se 78.96		35 Br 79.90		36 Kr 83.80	
39 Y 88.91		40 Zr 91.22		41 Nb 92.91		42 Mo 95.94		43 Tc (98)		44 Ru 101.1		45 Rh 102.9		46 Pd 106.4		47 Ag 107.9		48 Cd 112.4		49 In 114.8		50 Sn 118.7		51 Sb 121.8		52 Te 127.6		53 I 126.9		54 Xe 131.3											
57 La 138.9		72 Hf 178.5		73 Ta 180.9		74 W 183.8		75 Re 186.2		76 Os 190.2		77 Ir 192.2		78 Pt 195.1		79 Au 197.0		80 Hg 200.6		81 Tl 204.4		82 Pb 207.2		83 Bi 209.0		84 Po (209)		85 At (210)		86 Rn (222)											
89 Ac (227)		104 Rf (261)		105 Db (262)		106 Sg (266)		107 Bh (264)		108 Hs (269)		109 Mt (268)																													
		58 Ce 140.1		59 Pr 140.9		60 Nd 144.2		61 Pm (145)		62 Sm 150.4		63 Eu 152.0		64 Gd 157.3		65 Tb 158.9		66 Dy 162.5		67 Ho 164.9		68 Er 167.3		69 Tm 168.9		70 Yb 173.0		71 Lu 175.0													
		90 Th 232.0		91 Pa (231)		92 U 238.0		93 Np (237)		94 Pu (244)		95 Am (243)		96 Cm (247)		97 Bk (247)		98 Cf (251)		99 Es (252)		100 Fm (257)		101 Md (258)		102 No (259)		103 Lr (262)													

- Pairbreaking by magnetic impurities ($x_c < 1$ at%)

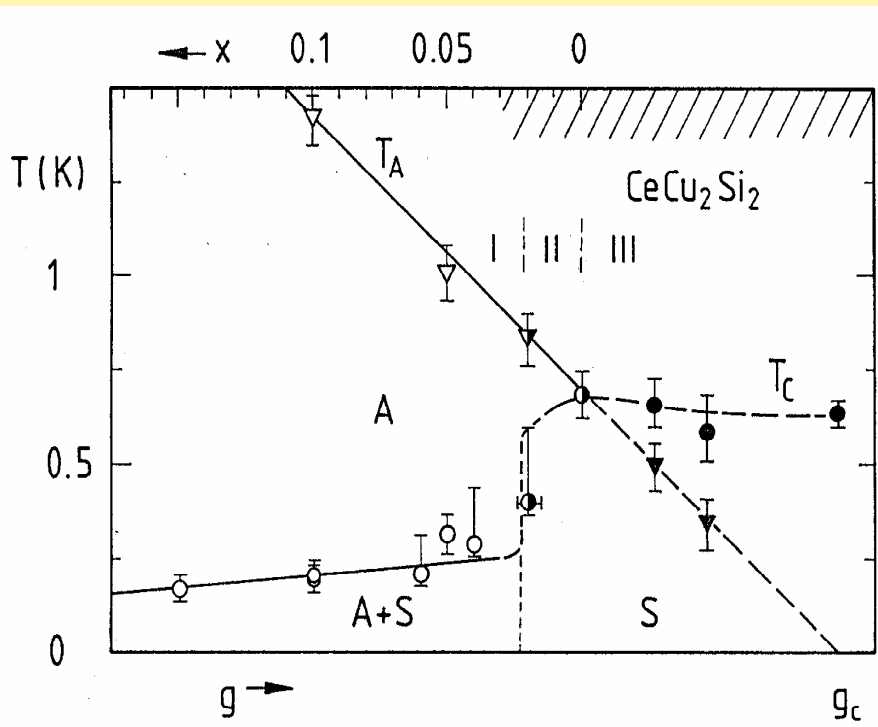
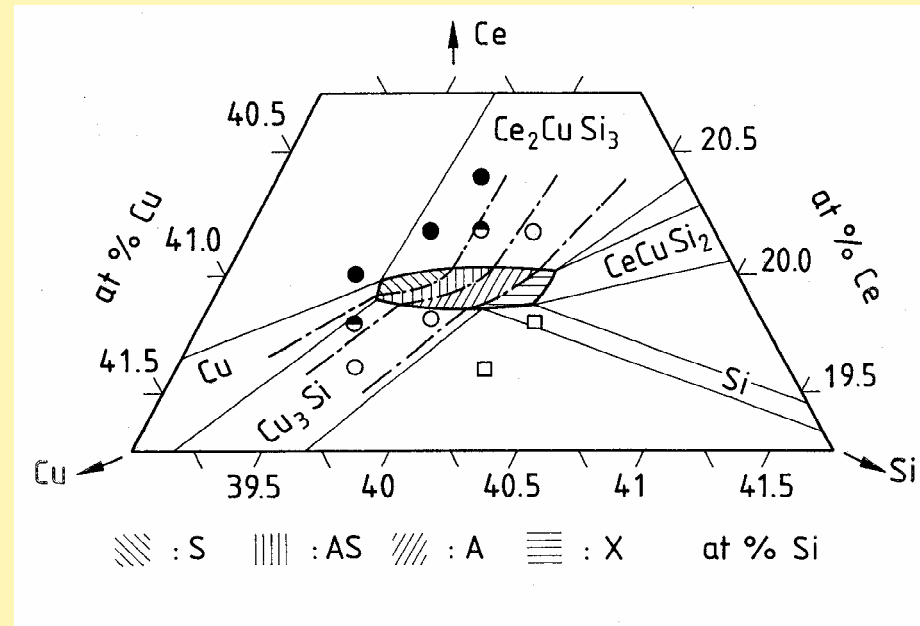
LaAl_2 $T_{C0} = 3.3$ K
 Gd-doping: $x_c = 0.6$ at%
 Ce-doping: $x_c = 0.9$ at%
 $T_K = 0.5$ K

(Riblet, Winzer 1971)



CeCu₂Si₂: Phase diagrams

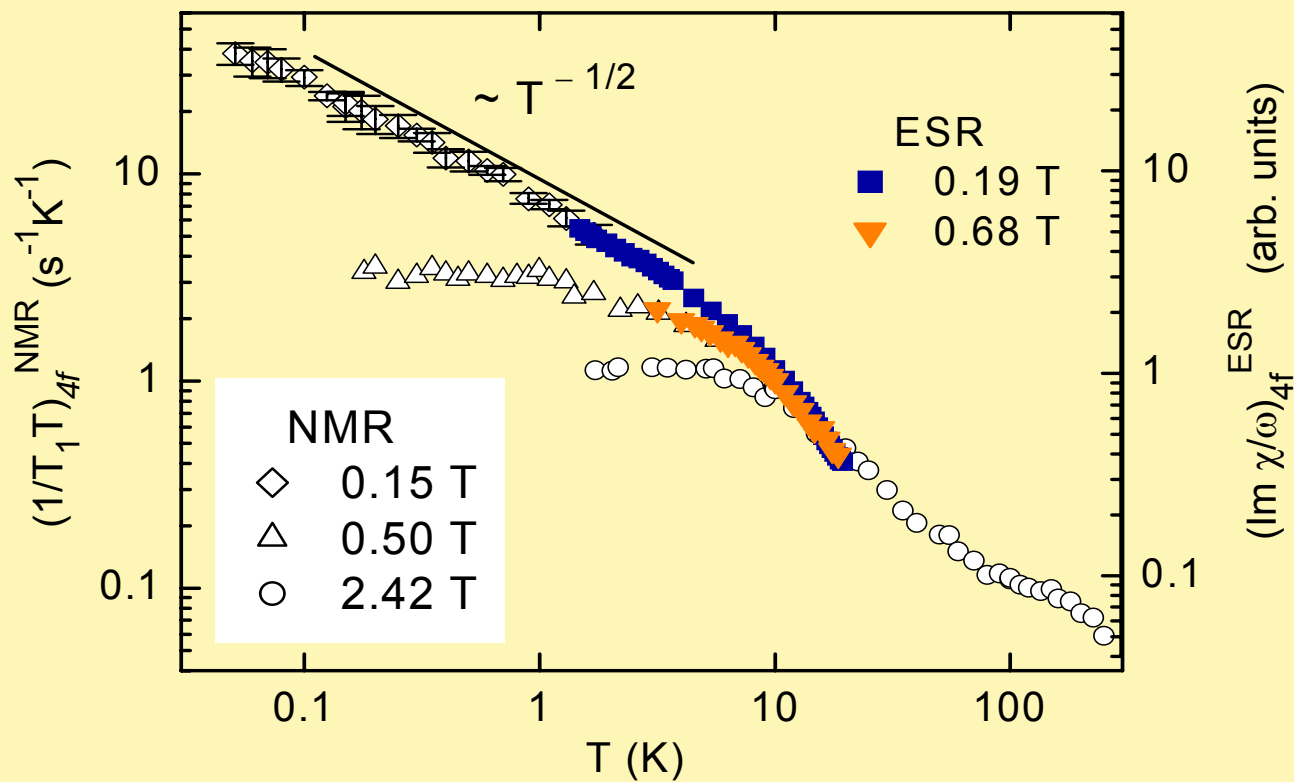
chemical (C. Geibel et al., 1995)



physical (P. Gegenwart et al., 1998)

^{29}Si NMR

[K. Ishida et al., PRL **89**, 107202 (2002)]



- $B > B_c$: LFL state below $T^*(B)$

- $\left\{ \begin{array}{l} B \rightarrow B_c^+ \\ T \rightarrow 0 \end{array} \right\} (1/T_1 T)_{4f} \propto T^{-1/2}$